

(Mathematics) (Syllabus)

M.Phil (Mathematics) COURSE-I

Time Allotted: 3 Hours.

Maximum Marks: 75.

Hydrodynamic and Hydromagnetic Stability-I

Introduction. Basic Concepts. Analysis in terms of normal modes. Non-dimensional number.

Benard Problem. Basic hydrodynamic equations. Boussinesq approximation. Perturbation equations. Analysis into normal modes. Principle of exchange of stabilities. Equations governing the marginal state. Exact solution when instability sets in as stationary convection for two free boundaries.

Thermal instability in rotating fluid. Perturbation equations. Analysis in terms of normal modes. Variational Principle for stationary convection. Solutions when instability sets in as stationary convection for two free boundaries. On the onset of convection as overstability; the solution for the case of two free boundaries.

Thermal instability in presence of magnetic field. Perturbation equations. The case when instability sets in as stationary convection; A variational principle. Solutions for stationary convection and for overstability for the case of two free boundaries.

Rayleigh-Taylor instability. Perturbation equations. Inviscid case. Effect of rotation. Effect of vertical magnetic field.

Text Books

1. Hydrodynamic and Hydromagnetic Stability, S. Chandrasekhar, Dover Publication, New York, 1981,

Chapter-1: § 1 to 4.

Chapter-II: § 5 to 12 & 15(a)

Chapter-III: § 24,25,26,27(a),29.

Chapter-IV: § 41,§:42, §43(a), §:44(a), §:46.

Chapter-X:§90,91,92,95,96.

M.Phil (Mathematics) COURSE-II

Time Allotted: 3 Hours.

Maximum Marks: 75.

Hydrodynamic and Hydromagnetic Stability-II

Initiation of Magnetoconvection

Review of the simple Bénard instability problem, Magnetohydrodynamic simple Bénard instability problem, The governing equations and Thompson's condition for the Exchange Principle. Extension of viscous case and Chandrasekhar's first method, Chandrasekhar's second method and his conjecture, A Sufficient condition for the exchange principle, Resolutions of Chandrasekhar's conjecture concerning the two energies, Solutions for the case when exchange principle is valid. Solutions for the case when overstability is valid, settlement of the recent controversy, Some illustrative examples.

Reformulation of the Simple Bénard and Thermohaline Instability Problem

Basis of the modified theory, Inadequacy of the classical theory, Construction of the modified, simplified governing equations, Modified equations for thermohaline instability problem, Modified Analysis of Simple Bénard instability problem and thermohaline instability problem, The eigenvalue problem, Characterization of the marginal state and the marginal state solution, Some illustrative examples.

Limitations of the Complex Wave Velocity in the Instability Problem of Heterogeneous Shear

Introduction, Governing Equations and initial stationary state solution, The perturbation equations, The normal mode analysis, The Mathematical eigenvalue problem and classification of modes, The origin of Kelvin-Helmholtz instability and Taylor's conjecture: Heuristic considerations The works of (a) Synge (1933), (b) Miles (1961), (c) Howard (1961). The problem of simultaneous reduction and unification, the work of Banerjee and Jain, A reduction theorem, The work of Kochar and Jain, An illustrative example.

Text book

1. Hydrodynamic and Hydromagnetic Stability, Mihir B. Banerjee and Jagdish, R. Gupta, Silver Line Publishers.

Chapter-I: § 1.1 to 1.9.

Chapter-II: §:2.1 to 2.8.

Chapter-III § 3.1 to 3.10



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M.Phil (Mathematics) COURSE-III

Time Allotted: 3 Hours.

Maximum Marks: 75.

Fluid Flow Instability, MHD, Plasmas and Geophysical Fluid Dynamics

Fluid Flow Instability

Kelvin-helmholtz instability, Perturbation equations and boundary conditions. Two uniform fluids in relative horizontal motion separated by a horizontal boundary. Discussions in the absence and presence of surface tension. Effect of rotation. Effect of horizontal magnetic field.

MHD and Plasmas

Magnetohydrodynamics (MHD). Introduction. Maxwell's equations for moving media, Magnetic induction equation and Maxwell's equations. Basic equations of MHD, Motion of a charged particle, General characteristics. The equations of motion of a charged particle in crossed electric and magnetic fields. The motion of a charged particle in a uniform magnetic field.

Geophysical Fluid Dynamics

Definition of porous medium. Porosity. Methods for measurement of porosity. Flow of homogeneous fluids in porous media. Darcy's law. Darcy's Oberbeck-Boussinesq (DOB) equations for material. Darcy's law further generalized. Basic equations of flow through porous media.

Text Books

1. Hydrodynamics and Hydromagnetic Stability, S. Chandrasekhar, Dover Publications, New York (1981), Chapter XI.
2. Stability of Fluid Motions II, D.D. Joseph, Springer-Verlag, New York (1976).
3. An Introduction to Magneto-Fluid Mechanics, V.C.A. Farraro and C. Plumpton, Oxford University Press (1966).
4. The Physics of Flow Through Porous Media, A.E. Schidegger University of Toronto Press, Toronto (1974).

hil(Mathematics) Course-IV.

Maximum Marks: 75.

GROUPS, RINGS AND MODULES

GROUPS & Ideals:

Characters of finite abelian groups, The Character group, the orthogonality relations for characters,

Maximal Ideal, Generators, Basic Properties of Ideals, Algebra of Ideals, Quotient Rings, Ideal in Quotient Rings, Local Rings.

The Jacobson Radical

Modules; The radical of a ring, Artinian rings, Semisimple Artinian rings.

Semisimple Rings

The density theorem, Semisimple rings, Applications of Wedderburn's theorem.

Text Books:

1. Introduction to Analytic Number Theory, Tom M. Apostol., Narosa Publishing House, New Delhi, Chapter-VI: Pages 129 to 136.
2. Non-Commutative Rings, I.N. Herstein, John Wiley and Sons, Inc., Chapters I&II, pages 1 to 68.
3. Introduction to Rings and Modules 2nd Edition, C. Musili, Narosa Publishing House, New Delhi; Chapter-II: Pages 33 to 65.

M.Phil(Mathematics) Course No.-V

Time Allotted:3 Hours.

Maximum Marks: 75.

MATRIX ANALYSIS

Matrices, Partioned Matrices, Special types of matrices, Change of basis, ,Similarity.Unitary Matrices, Unitary equivalence, Schur's unitary triangularization theorem, Some implications of Schur's theorem. Normal Matrices. Definitions, Properties and characterizations of Hermitian Matrices. Canonical forms , The Jordan Canonical form: proof observations and applications.Variational characterization of eigenvalues of Hermitian Matrices. Some applications of the Variational characterizations.

Positive definite matrices, Definitions and properties, characterization. The polar form and the singular value decomposition. Genaralised inverse. Inequalities for the positive definite matrices.

Matrix Norms. Symmetric Norms. Norms on \mathbb{C}^n . Unitarily Invariant norms on operators \mathbb{C}^n . Lidskii's theorem (third proof).

Books

1. Matrix Analysis: Roger A. Horn and Charles R. Johnson. Cambridge University Press, Reprinted 1988.

Chapter 0 0.2, 0.7, 0.9, and 0.10

Chapter 1 1.3

Chapter 2 2.0-2.5

Chapter 3 3.0, 3.1, 3.2 (3.2.1 and 3.2.3)

Chapter 4 4.0-4.3

Chapter 5 5.6 and 5.7.

Chapter 7 7.0, 7.1, 7.2, 7.3 and 7.8

2. Matrix Analysis: Rajendra Bhatia, Springer-Verlag, New York, Inc. 1997.

Chapter-IV: IV.1-IV.5

OF M.PHIL(Mathematics) Course-VI

Time Allotted:3 Hours.

Maximum Marks: 75.

BOUNDARY-LAYER THEORY

CHAPTER-XIV: **BOUNDARY-LAYER CONTROL IN LAMINAR FLOW:**

(A) Methods of boundary-Layer Control.

1. Motion of the solid wall.
2. Acceleration of the boundary layer (blowing).
3. Suction
4. Injection of a different gas.
5. Prevention of transition by the provision of suitable shapes. Laminar aerofoils.
6. Cooling of the wall.

(B) Boundary-Layer suction.

1. Theoretical results.
 - 1.1. Fundamental equations
 - 1.2. Exact solutions
(Flat plate: Boundary Layer with pressure gradient)
Approximate Solutions

(C) Injection of a different gas (Binary boundary Layers)

- 1.1 The fundamental equations.

CHAPTER XV: **NON-STEADY BOUNDARY LAYERS.**

(A) Basic Equations:

1. Boundary layer equations.
2. The Method of successive approximations.
3. C.C.Lin's Method for periodic external flows.
4. Expansion into a series when a steady stream is perturbed slightly.
5. Similar and semi-similar solutions.
6. Approximate solutions.

(B) Boundary-Layer formation after impulsive start of motion.

1. Two-dimensional case.
2. Axially symmetrical problem.

(c) Boundary-Layer formation in accelerated motion.

(e) Periodic boundary-layer flows.

1. Oscillating cylinder in fluid at rest.



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f harmonic oscillations.
small, harmonic perturbation boundary-layer theory.

PERTURBATION METHODS

Parameter perturbation, co-ordinate perturbation, order symbols and Gauge functions, asymptotic expansions and sequences. Convergent versus Asymptotic series, Non Uniform expansions.

Books:

1. Boundary-Layer Theory, Dr. Hermann Schlichting, Mc GRAW-HILL Book Company, New York.
2. Perturbation Methods, A.N. Nayfeh, A Willey-Inter science Publication.



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Department of Mathematics*
"Himachal Pradesh University"
Summer-Hill, Shimla-171 005.

No.1-2/2000-HPU(Maths)
Dated: 03.12.2008.

From:

The Chairman,
Department of Mathematics,
H.P.University, Shimla-171 005.

To

The Assistant Registrar (Admn.)
(General Administration Section),
H.P.University, Shimla-5.

Sub: **Regarding Celebration of "Quami Ekta Week"-2008."**
Sir,

This is with reference to AR (Teaching) letter number 1-8/2008-
HPU(DS) dated 22nd November, 2008 regarding celebration of Quami Ekta
Week-2008 enclosing herewith 35 flags to distribute the same amongst the
Teaching/Non-Teaching staff/students.

Please find enclosed herewith Rs.100/- (Rs. Hundred only)
collected from the Teaching/Non-Teaching staff and students of the
Department alongwith remaining 15 flags of Quami Ekta Week-2008 for
taking further necessary action.

Yours faithfully,

(M.G.Gourla)
Professor & Chairman.

Copy to:

The Dean of Studies, H.P.University, and Shimla-5 for information
please.

(M.G.Gourla)
Professor & Chairman.



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**Department of Mathematics*
“Himachal Pradesh University”
Summer-Hill, Shimla-171 005.*

*No.1-10/2004-HPU(Maths)
Dated: 03.12.2008.*

From:

The Chairman,
Department of Mathematics,
H.P.University, Shimla-171 005.

To

*The Dean of Studies,
Himachal Pradesh University,
Summer-Hill, Shimla-171 005.*

Sub: *Printing of Handbook of Information for the session 2009-2010.*

Sir,

reference to your Office letter Number HBI/2008-2009/- dated 24 November, 2008 on the subject cited above. In this connection I have to inform you that the list of Faculty Members in the Handbook of Information for the session 2009-2010 in the Department of Mathematics will be changed as under:

| <i>Sr. No.</i> | <i>Names</i> | <i>Designation</i> |
|----------------|------------------------------|---------------------------------|
| 1. | <i>Dr.M.G.Gourla</i> | <i>Professor & Chairman</i> |
| 2. | <i>Dr.R.G.Shandil</i> | <i>Professor</i> |
| 3. | <i>Dr.R.P.Sharma</i> | <i>Reader</i> |
| 4. | <i>Dr.(Mrs.)Veena Sharma</i> | <i>Reader</i> |
| 5. | <i>Dr.J.S.Dhiman</i> | <i>Reader</i> |
| 6. | <i>Dr.Rajesh Sharma</i> | <i>Reader</i> |

Yours faithfully,

(M. G. Gourla)

Professor & Chairman

SYLLABUS OF M.PHIL(Mathematics) Course-VI

CHAPTER-XIV: **BOUNDARY-LAYER CONTROL IN LAMINAR FLOW:**

(B) Methods of boundary-Layer Control.

7. Motion of the solid wall.
8. Acceleration of the boundary layer (blowing).
9. Suction
10. Injection of a different gas.
11. Prevention of transition by the provision of suitable shapes. Laminar aerofoils.
12. Cooling of the wall.

(B) Boundary-Layer suction.

2. Theoretical results.
 - 1.1. Fundamental equations
 - 1.2. Exact solutions

(Flat plate: Boundary Layer with pressure gradient)

Approximate Solutions

(C) Injection of a different gas (Binary boundary Layers)

equations.

CHAPTER XXV. NON-STEADY BOUNDARY LAYERS

7. Boundary óLayer equations.
8. The Method of successive approximations.
9. C.C.Lin's Method for periodic external flows.
10. Expansion into a series when a steady stream is perturbed slightly.
11. Similar and semi-similar solutions.
12. Approximate solutions.

(B) Boundary-Layer formation after impulsive start of motion.

1. Two-dimensional case.
2. Axially symmetrical problem.

(c) Boundary-Layer formation in accelerated motion.

(e) Periodic boundary-layer flows.

1. Oscillating cylinder in fluid at rest.
2. C.C.Lin's theory of harmonic oscillations.
3. External flow with small, harmonic perturbation boundary-layer theory

PERTURBATION METHODS

Parameter perturbation, co-ordinate perturbation, order symbols and Gauge functions, asymptotic expansions and sequences. Convergent versus Asymptotic series, Non Uniform expansions.

Books:

1. Boundary-Layer Theory, Dr. Hermann Schlichting, Mc GRAW-HILL Book Company, New York.
2. Perturbation Methods, A.N. Nayfeh, A Willey-Inter science Publication.

CONTENTS

Section-A, Revenue Account, III-Research Project,

Department of Mathematics & Statistics, HPU, Shimla.

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| 4. | Dr.(Mrs.)Veena Sharma Reader | To |
| 5. | Dr. Joginder Singh Dhiman, Reader | To |
| 6. | Dr.Rajesh Sharma, Reader | To |
| 7. | | To |